



# From Bell's theorem to secure key distribution

**Nicolas Gisin, Valerio Scarani**, Geneva

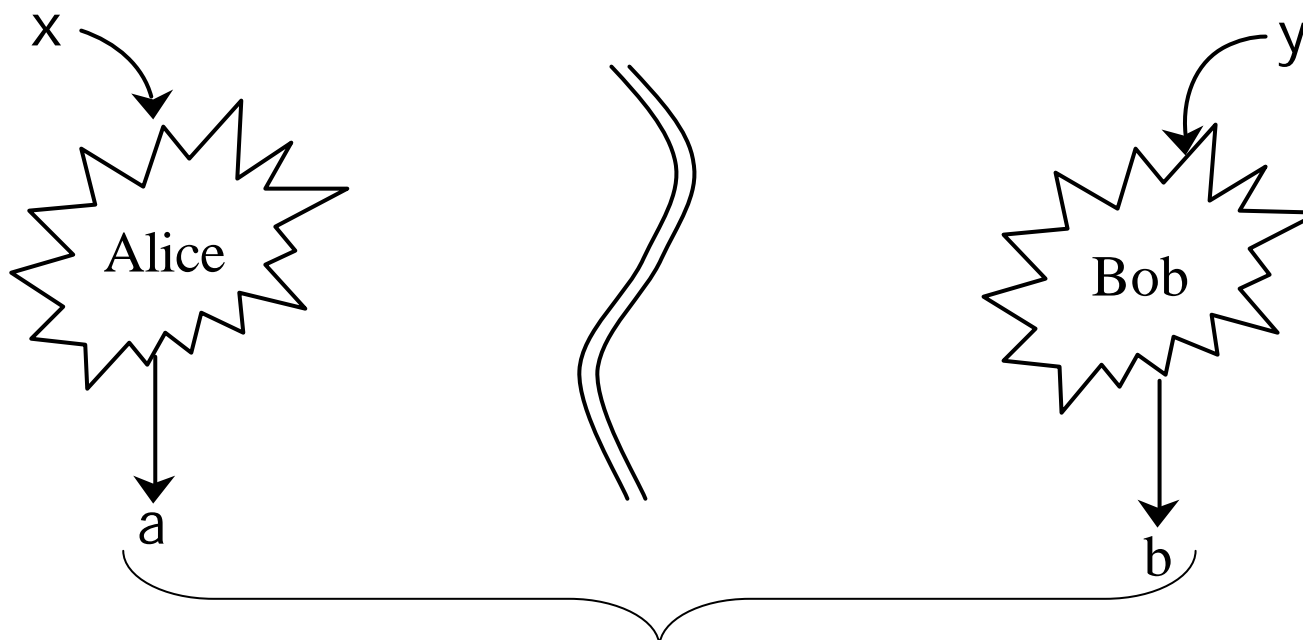
**Antonio Acin**, Barcelona

**Lluís Masanes**, Bristol

- Key distribution: abstract setting
- Assumptions in security proofs of “unconditional” QKD
- Security against individual attacks from no-signaling
- Heisenberg uncertainty for non-signaling correlations



## Key distribution: abstract setting



assumptions  
about Eve's  
power

$$P(a, b | x, y)$$

$$P(a, b, e | x, y, z)$$

key distillation  $\mathbb{P}$  secret key



# Assumptions in security proofs of "unconditional" QKD

$$P(\underbrace{a, b}_{\text{measurements outcomes}} \mid \underbrace{x, y}_{\text{bases choices}})$$

measurements outcomes      bases choices

Example of BB84:  $P(a=b|x=y) \approx 1$

Eve's power limited only by quantum laws       ~~$\Rightarrow$  secure secret key~~  
and Alice and Bob's Q systems are       $\Rightarrow$  secure secret key  
2-dimensional

$$\frac{1}{4}(|0,0\rangle_{ab}\langle 0,0| + |1,1\rangle_{ab}\langle 1,1|) \otimes (|0,0\rangle_{ab}\langle 0,0| + |1,1\rangle_{ab}\langle 1,1|)_x$$

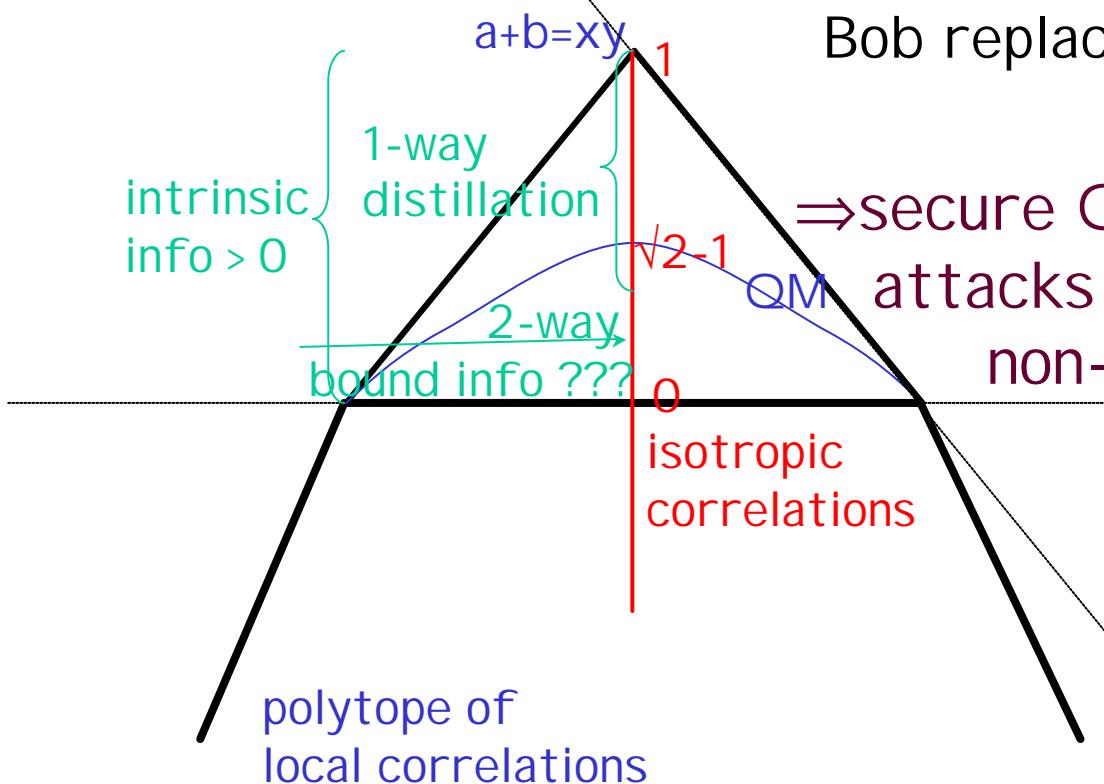
This is a real threat to actual implementations of QKD,  
known as « side channels ».



# Security against individual attacks from no-signaling

[J.Barrett et al, PRL'05](#)  
[A.Acin, L.Masanes, NG](#)  
[quant-ph/0510094](#)

facet corresponding to the no-signaling  $\leq$ :



Eve distributes the correlation.  
 For each realization she produces one of the vertices with fixed prob.

The protocol (pseudo-sifting):

Alice announces her  $x$

Bob always accepts

Bob replaces his  $b$  with  $b+xy$

$\Rightarrow$  secure QKD against individual attacks by any post-quantum non-signaling Eve !

facet corresponding to the CHSH-Bell  $\leq$ :  
 $\sum P \leq 3$

# Security against individual attacks from no-signaling



GAP Optique Geneva University

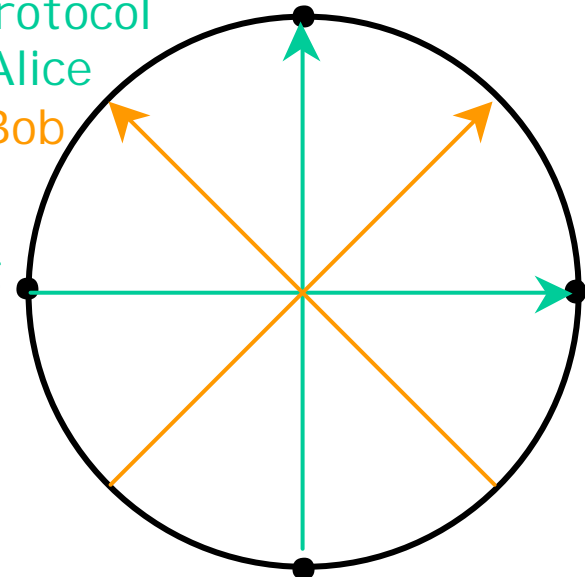
A.Acin, L.Masanes, NG  
quant-ph/0510094

CHSH Q-crypto protocol

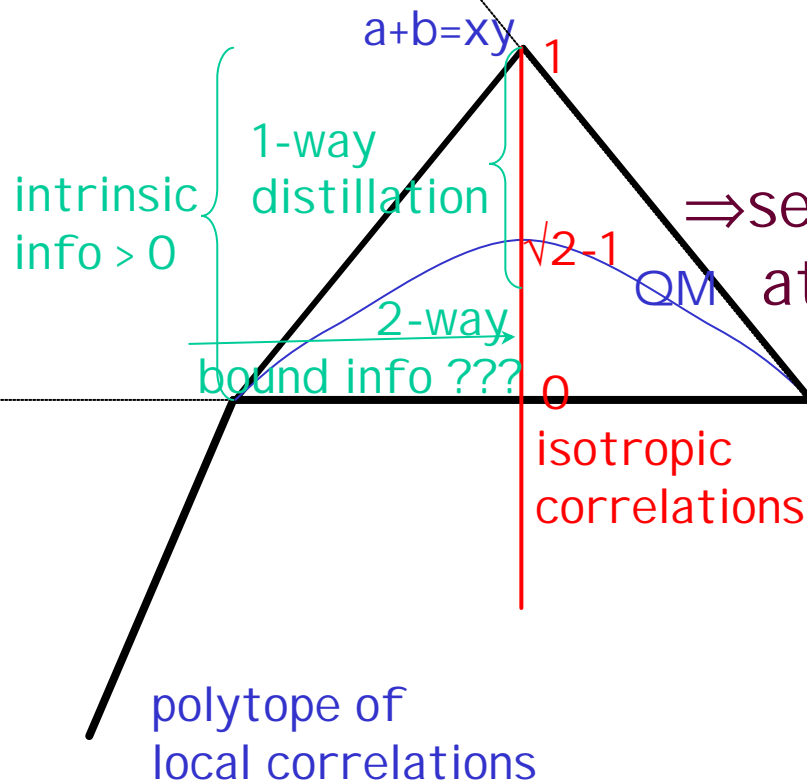
Alice  
Bob

pseudo-sifting:

- 1-way
- all bits are kept
- noisy even without Eve



facet corresponding to the no-signaling  $\leq$ :



$\Rightarrow$  secure QKD against individual attacks by any post-quantum non-signaling Eve !

facet corresponding to the CHSH-Bell  $\leq$ :  
 $\sum P \leq 3$



# Heisenberg uncertainty for non-signaling correlations

QBER for a given input  $x$  on Alice side:  $Q_x = P(a \neq b | x)$

Eve's information gain:  $I(E, B | x)$

Information gain versus disturbance trade-off:

$$I(E, B | x=0) = \frac{1}{2} Q_{x=1}$$

$$I(E, B | x=1) = \frac{1}{2} Q_{x=0}$$



# Conclusions

- Correlations that do not violate any Bell inequality can not be distilled to a secret key without assumptions on the Hilbert space dimensions.
- Any correlation that violates some Bell inequality has a positive intrinsic information.
- In the binary case, security is proven against individual attacks for most nonlocal correlations, including some Q correlations.
- In the binary case, the Heisenberg trade-off bw information gain and disturbance holds for all non-signaling correlations.